# **University of Houston-Downtown**

### Course Prefix, Number, and Title: MATH 1301: College Algebra

### Credits/Lecture/Lab Hours: 3/3/0

### Foundational Component Area: Mathematics

**Prerequisites:** Prerequisites: A grade of C or better in MATH 1300 or a TSI score of 350 or higher. **Co-requisites:** None

**Course Description:** College-level topics in algebra including variation, systems of equations, nonlinear inequalities, functions and their graphs, lines, quadratic equations and functions, complex numbers, polynomials, exponential and logarithmic functions, the algebra of functions, and applications related to these topics.

### TCCNS Number: MATH1314

#### Assigned Core Learning Outcome Instructional strategy or Method by which Objective Students will be able to: content used to achieve the students' mastery of outcome\* this outcome will be evaluated Critical Thinking Describe and **Content:** Functions and their Final Exam and Online Homework which communicate representations; types of mathematical information functions and their rates of Communication include: verbally, numerically, change; percent change; 1. Open-ended Empirical & graphically, and linear functions and models; discussion Quantitative symbolically. absolute values; quadratic questions where Reasoning functions, power functions, students have to exponential and logarithmic discuss functions. mathematical information or Instructional Strategies: data; Asking students to convert 2. Questions different representations of requiring functions into each other, find students to slope, x-intercept, y-intercept, create, analyze vertex, power laws, simplify and interpret and evaluate symbolic graphs and expressions, graph functions, charts; solve equations. 3. Peer-to-peer activity, where students should explain to each

### Demonstration of Core Objectives within the Course:

|                   |                             |                                      | other orally          |
|-------------------|-----------------------------|--------------------------------------|-----------------------|
|                   |                             |                                      | their solution to     |
|                   |                             |                                      | a mathematical        |
|                   |                             |                                      | problem and/or        |
|                   |                             |                                      | concepts from a       |
|                   |                             |                                      | particular topic      |
|                   |                             |                                      | in mathematics.       |
| Critical Thinking | Use appropriate             | Content: Linear, quadratic,          | Final Exam and Online |
|                   | mathematical techniques     | piecewise, and power                 | Homework.             |
| Empirical &       | to model situations from a  | functions and models;                |                       |
| Quantitative      | variety of settings,        | midpoint formula; percent            |                       |
| Reasoning         | including real-world        | change; problem solving in           |                       |
|                   | applications in generalized | applications.                        |                       |
|                   | mathematical forms.         |                                      |                       |
|                   |                             | Instructional Strategy: Asking       |                       |
|                   |                             | students to extrapolate and          |                       |
|                   |                             | interpolate data, convert data       |                       |
|                   |                             | given by graphs and tables           |                       |
|                   |                             | into equations, interpret and        |                       |
| <b></b>           |                             | classify real-world data sets.       |                       |
| Critical Thinking | Interpret mathematical      | <b>Content:</b> Interpret parameters | Final Exam and Online |
|                   | models, such as formulas,   | of linear, quadratic, piecewise,     | Homework.             |
| Empirical &       | graphs, tables, and         | power, exponential and               |                       |
| Quantitative      | schematics, and draw        | logarithmic functions                |                       |
| кеазопіпд         | interences from them.       | occurring in applications,           |                       |
|                   |                             | determine characteristics of         |                       |
|                   |                             | model behavior using the             |                       |
|                   |                             | properties of functions and          |                       |
|                   |                             | their graphs (slopes,                |                       |
|                   |                             | intercepts, local extrema,           |                       |
|                   |                             | etc.).                               |                       |
|                   |                             | Instructional Strategies:            |                       |
|                   |                             | Online homework questions            |                       |
|                   |                             | asking students to convert           |                       |
|                   |                             | formulas graphs and tables           |                       |
|                   |                             | into qualitative descriptions        |                       |
| Critical Thinking | Discern relationships and   | <b>Content:</b> Fit given data to    | Final Exam and Online |
| 5                 | patterns in quantitative    | linear, quadratic, piecewise         | Homework.             |
| Empirical &       | data to arrive at informed  | power, exponential and               |                       |
| Quantitative      | conclusions.                | logarithmic functions.               |                       |
| Reasoning         |                             | extrapolate and interpolate          |                       |
|                   |                             | based on the fit. construct          |                       |
|                   |                             | simple models based on               |                       |

|                   |                           | informal descriptions.            |                           |
|-------------------|---------------------------|-----------------------------------|---------------------------|
|                   |                           | Instructional Strategies:         |                           |
|                   |                           | Asking students to translate      |                           |
|                   |                           | text descriptions of applied      |                           |
|                   |                           | problems and quantitative         |                           |
|                   |                           | data into tables, graphic and     |                           |
|                   |                           | analytic representations, use     |                           |
|                   |                           | these representations to          |                           |
|                   |                           | optimize parameters, predict      |                           |
|                   |                           | behavior or fill in missing data. |                           |
| Critical Thinking | Utilize appropriate       | Content: Nonlinear functions      | Final Exam and Online     |
|                   | technology to enhance     | and equations: features of        | Homework which            |
| Empirical &       | mathematical thinking and | graphs, generalizing based on     | include problems          |
| Quantitative      | understanding, to solve   | features of graphs                | requiring students to     |
| Reasoning         | mathematical problems,    | (relationships between            | use graphing utilities to |
|                   | and to judge the          | turning points, extrema and       | find a solution.          |
|                   | reasonableness of the     | direction of increase);           |                           |
|                   | results.                  | introduction to functions and     |                           |
|                   |                           | graphs—choosing the               |                           |
|                   |                           | appropriate viewing window;       |                           |
|                   |                           | solving quadratic inequalities;   |                           |
|                   |                           | solving optimization problems     |                           |
|                   |                           | using a graph.                    |                           |
|                   |                           |                                   |                           |
|                   |                           | Instructional Strategy: Asking    |                           |
|                   |                           | students to analyze and           |                           |
|                   |                           | answer questions about            |                           |
|                   |                           | graphing calculator plots;        |                           |
|                   |                           | choose the appropriate            |                           |
|                   |                           | viewing window for a              |                           |
|                   |                           | function; trace intercepts and    |                           |
|                   |                           | extrema; use graph to solve       |                           |
|                   |                           | quadratic inequalities.           |                           |

### Additional Course Outcomes:

- Interpret and use functional notation, express concepts and properties in functional notation, recognize and apply different types of functions including linear, polynomial, exponential and logarithmic.
- Determine key properties of functions from various representations, convert among the representations, and recognize common properties of different functions.
- Solve linear, quadratic and absolute value equations and inequalities, interpret solutions.

- Interpret numerical data and construct simple models, interpolate and extrapolate data, evaluate the meaning of results.
- Use graphing utilities to graph functions, solve equations, visualize and interpret data.
- Demonstrate mathematical reasoning skills and skills for presenting mathematical concepts and arguments.

### **Course Outline:**

- Unit I Introduction to Functions and Graphs (7 hours)
  - Review sets of numbers; visualization of data; relations, functions, and their representations; the Midpoint Formula; function notation and its practical interpretation; types of functions and their rates of change; interval notation; where a function is increasing and decreasing; percent change.
  - <u>Optional:</u> Setting the viewing window on a graphing calculator; making a scatter plot on the graphing calculator representing a function on a graphing calculator.
- Unit II Linear Functions and Equations (7 hours)
  - Topics or techniques to be covered include: Linear functions and models; equations of lines; linear equations; intercepts and their practical interpretation; linear inequalities; piecewise-defined functions; absolute value equations; absolute value inequalities; direct variation;
  - <u>Optional</u>: Locating a zero of a function on a graphing calculator, applying the intersection of graphs method of solving equations (); solving equations with technology.
- Unit III Quadratic Functions and Equations (7 hours)
  - Quadratic functions and models; quadratic equations and problem solving; quadratic inequalities; complex numbers. Solving equations with technology; solving quadratic inequalities with technology.
- Unit IV Nonlinear Functions and Equations (7 hours)
  - Review all topics from prerequisite courses as needed; nonlinear functions and their graphs; polynomial functions and models; fundamental properties of polynomials; the Fundamental Theorem of Algebra. Discussion of rational functions and models as time permits. Discussion of inverse proportion (and polynomial and rational inequalities only as time permits).
  - <u>Optional:</u> Finding extrema on the graphing calculator.
- Unit V Exponential and Logarithmic Functions (7 hours)
  - Combining functions with algebraic operations; decomposing functions; inverse functions and their representations; inverse function notation and its practical interpretation; exponential functions and models; logarithmic functions and models; properties of logarithms; exponential and logarithmic equations. Instructors are strongly encouraged to have students use calculators during this unit. Discuss constructing nonlinear models only as time permits.
  - <u>Optional:</u> Graphing an inverse function; solving an exponential equation graphically.

- Unit VI Systems of Equations and Inequalities (3 hours)
  - Review or discuss functions and equations in two variables; systems of equations and inequalities in two variables as needed. Systems of linear equations in three variables.
- **Peer-Interview Activity** (1 hour)
  - Students will be paired up to participate in a peer-interview about a particular topic in mathematics. Choice of a topic and the specifics are left to the instructor.

## Grading/Course Content which Demonstrates Student Achievement of Core Objectives:

The grading scale is as follows: 100-90% = A; 89-80% = B; 79-70% = C; 69-60% = D; 59-0% = F.

| Summary of Course Exams, Quizzes, Assignments and Final                            |                    |  |  |  |
|--|--------------------|--|--|--|
| Three in-class tests (15%/exam)  | 45% of final grade |  |  |  |
| Quizzes  | 15% of final grade |  |  |  |
| Homework and in-class activities   | 7% of final grade  |  |  |  |
| including written and oral assignments.  |                    |  |  |  |
| Final  | 33% of final grade |  |  |  |
| NOTE: If the final exam score is less than 50, the student will receive an "F" for |                    |  |  |  |
| the course regardless of his or her average.                                       |                    |  |  |  |